

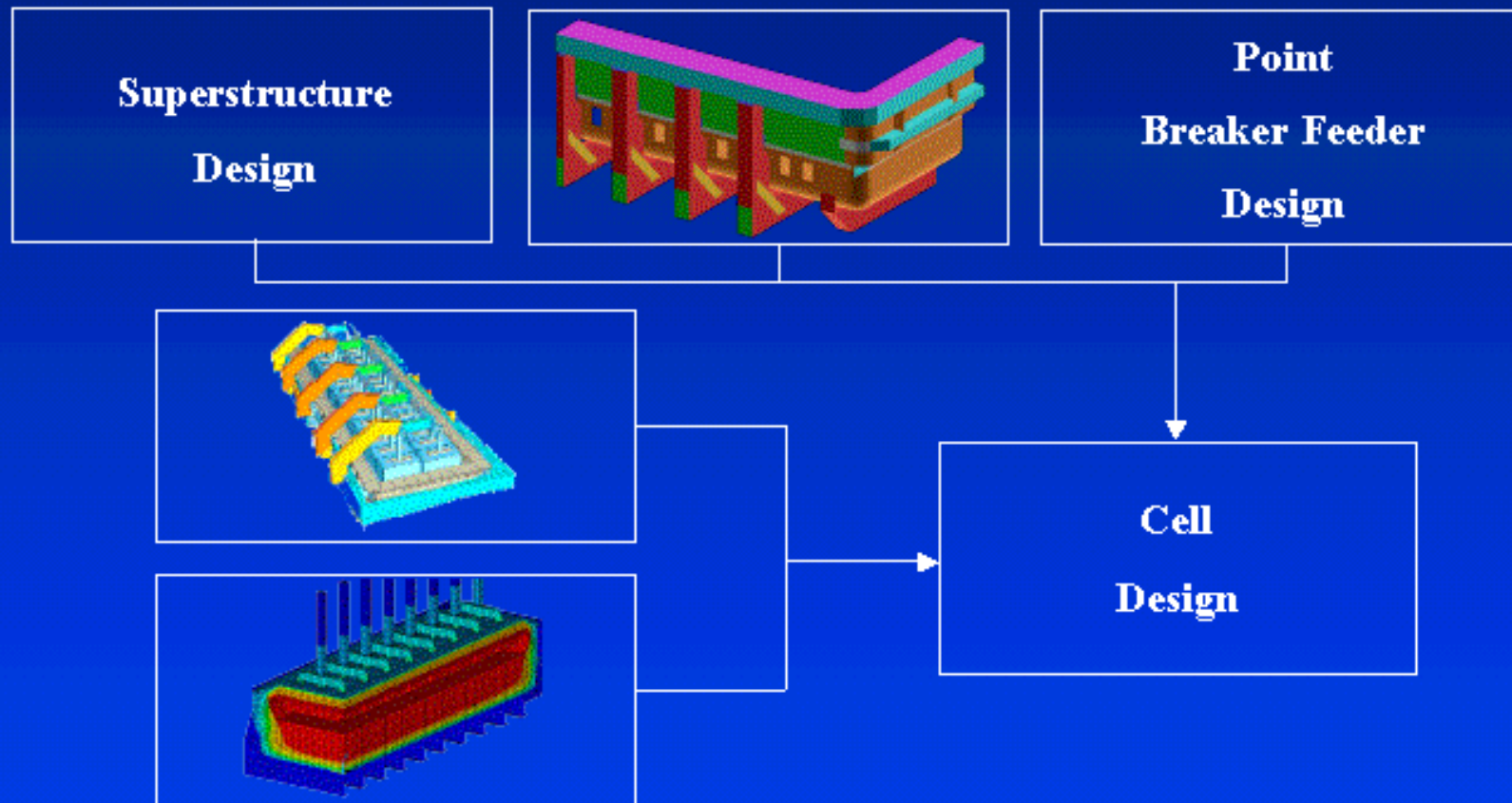
Industrial Aluminum Electrolysis

Marc Dupuis Process Simulation

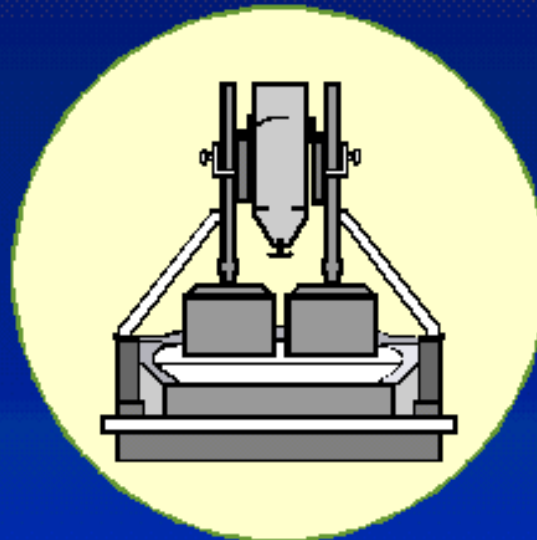
GENISIM

GENISIM

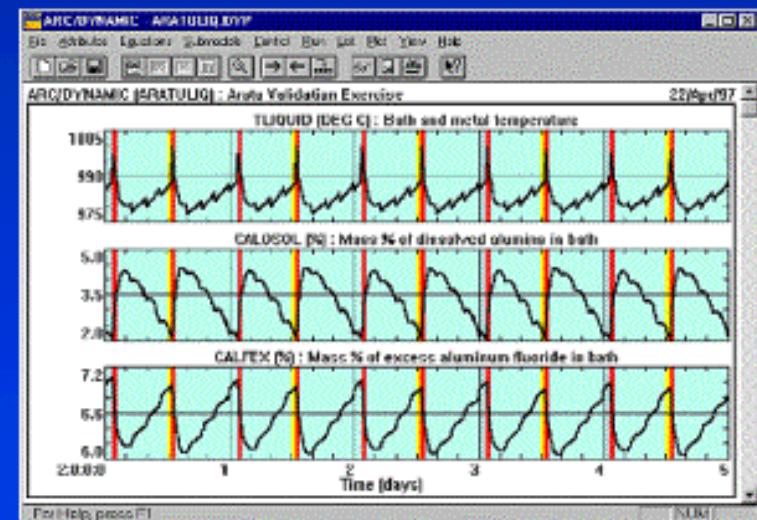
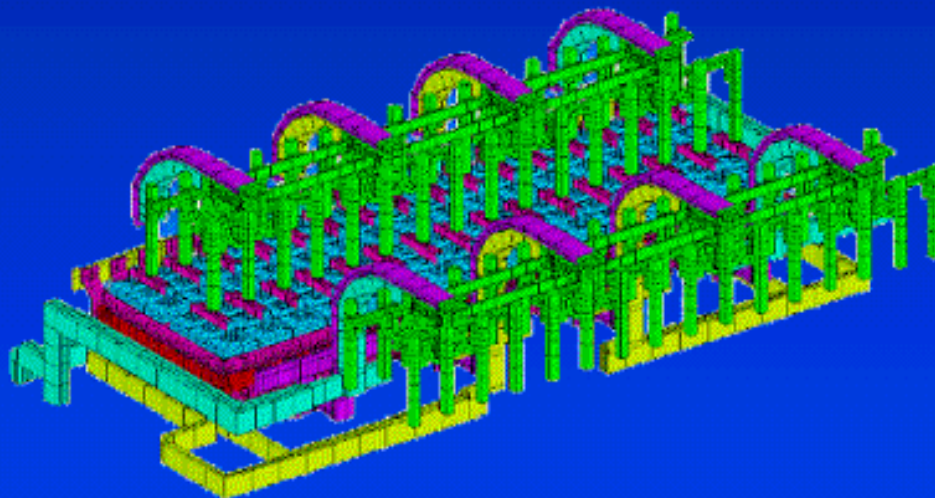
Categories of Hall-Hérault Mathematical Models



**3D
Steady-State
Models**



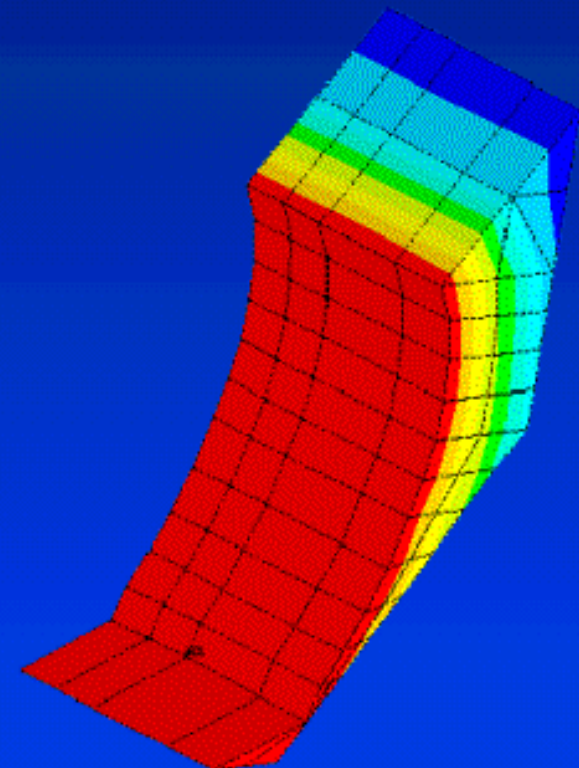
**1D
Dynamic
Models**



GENTSIM

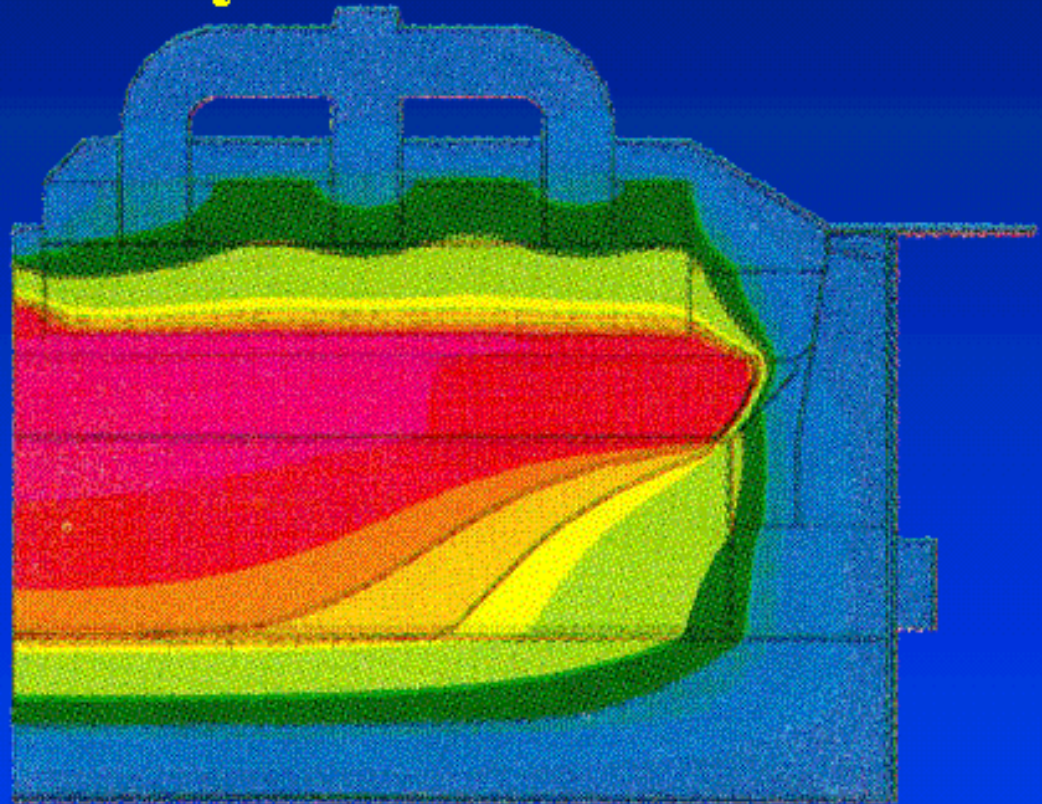
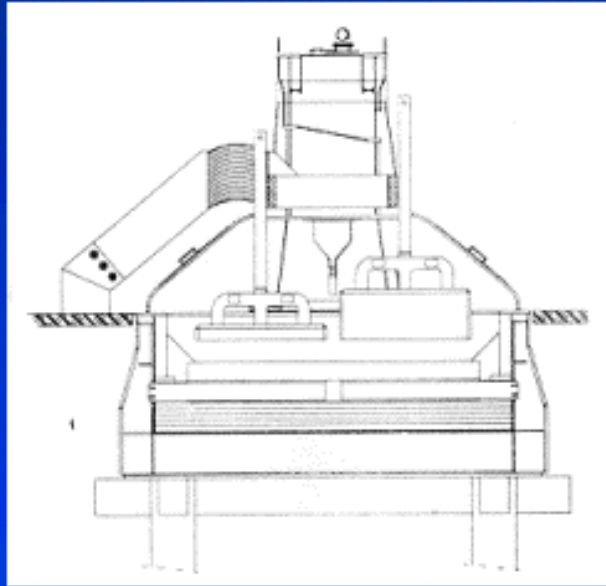
The Goals of 3D Steady-State Thermal-Electric Models are to Calculate the:

- Global Cell Heat Dissipation
- Cathode Lining Drop
- Ledge Profile
- Anode Drop



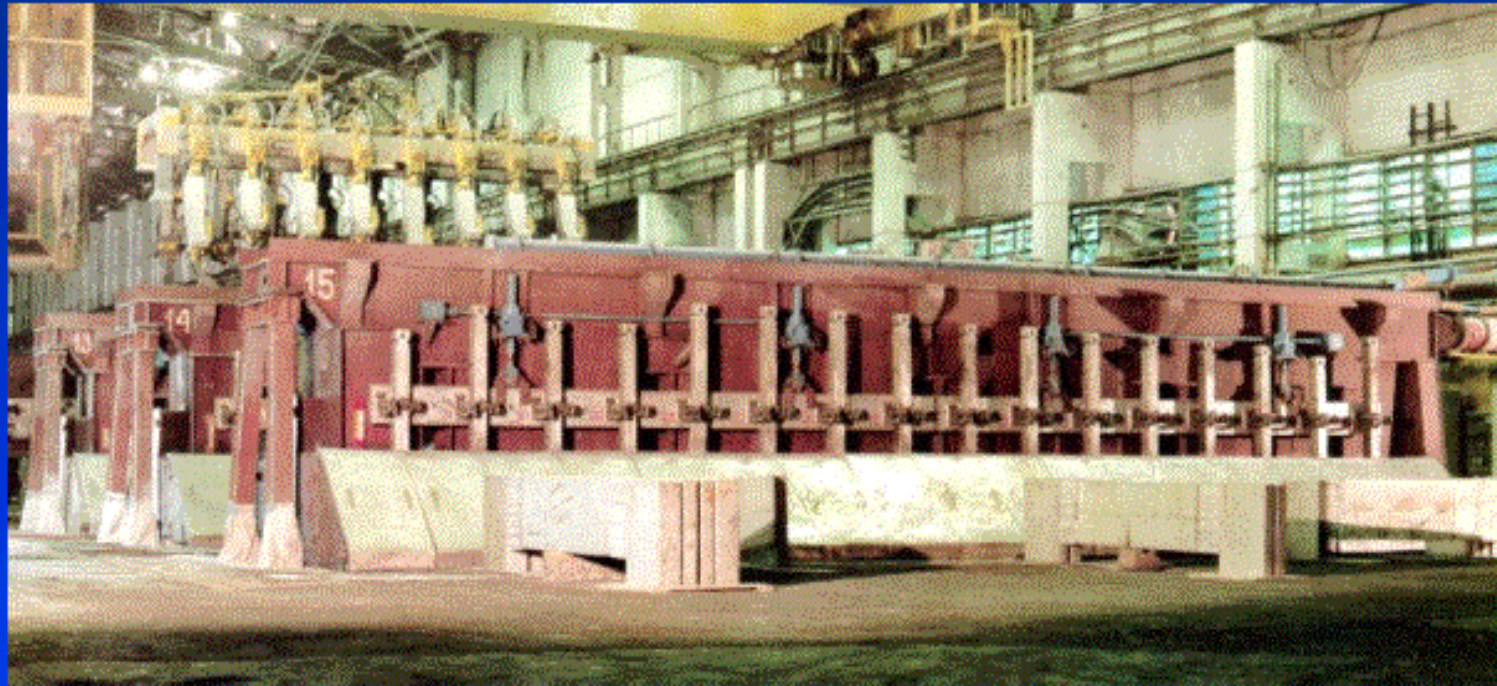
GENISIM

Demonstration Models Inspired from the VAW's JOM Paper of February 1994



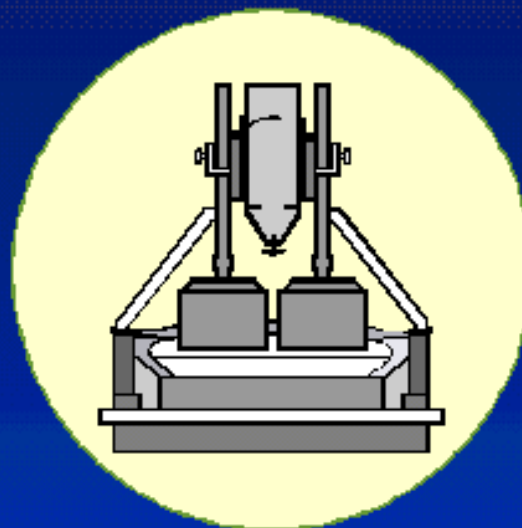
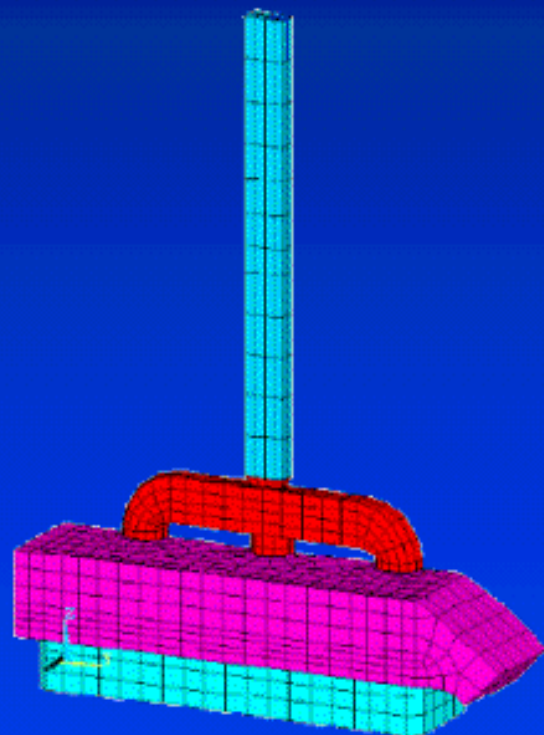
GENTSIM

I used the Information Available and Guessed the Rest, so it is a Realistic but *Imaginary* Cell Design

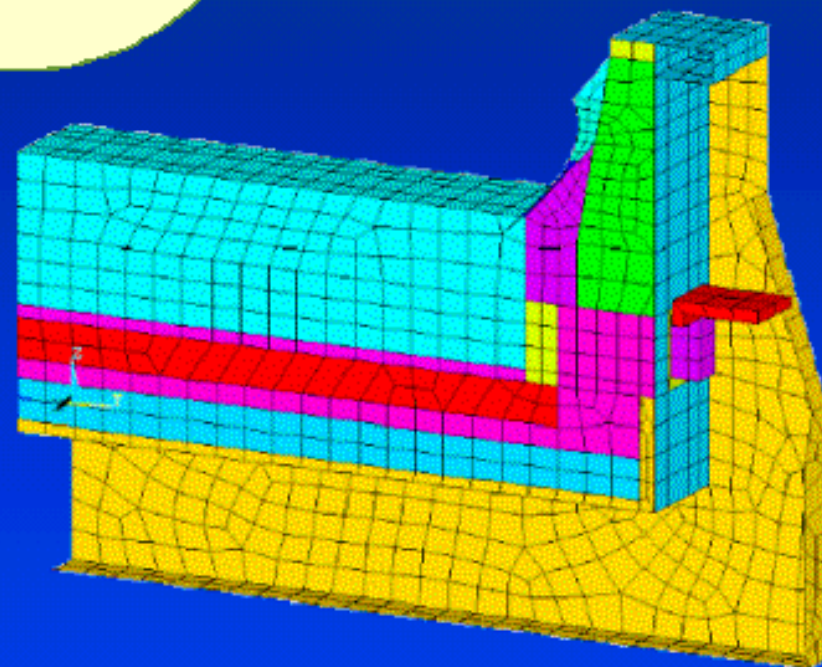


GENTSIM

**Half-Anode
Model**



**Cathode
Side Slice
Model**



GENISIM

Thermal Blitz

Heat Flux Measurements for Cell Heat Balance		
date:	8-Sep-97	slice no: A2
cell:	"GAP" 300	
Shell Wall		
Description	Flux	Temp
Wall above shell level	2000	130
Wall deck level	5500	230
Wall metal level	7300	230
Wall block level above bar	6000	235
Wall concrete bar	5000	190
Right collector bar	3000	190
Wall concrete bar level	1300	80
Wall deck level	1000	60
Flange near centerline	300	30
Flange at quarter point	500	50
Flange near corner	300	30
Cradle web		
Wall above shell level	1000	100
Wall deck level	2165	130
Wall metal level	2880	190
Wall block level above bar	955	125
Wall concrete bar level	900	80
Wall deck level	155	50
Flange extension	0	0
In line corner	100	35
Wall extension above section	0	0
Wall extension above section	0	0
Flange near centerline	100	35
Flange at quarter point	100	35
Flange near corner	100	35
Cradle flange		
Wall above deck level	300	65
Wall deck level	1085	80
Wall metal level	1550	90
Wall block level above bar	475	90
Wall concrete bar level	200	55
Wall deck level	50	30
Flange line flange	30	30

Heat Balance Results

date: 8-Sep-97

Cell: "GAP" 300

Cathode Heat Losses

	Wt ml	kW	%
Shell side wall above bath level	1000	11.51	1.86
Shell side wall opposite to bath	5500	11.68	5.11
Shell side wall opposite to metal	7500	11.10	6.97
Shell side wall opposite to block above bar	6000	11.18	7.80
Shell side wall opposite to block between bars	1500	6.18	1.05
Collector bars to air	1000	17.18	1.79
Collector bars to flexible	60	6.0	9.68
Shell side wall opposite to brick	1000	11.51	1.86
Shell floor close to corner	500	12.51	1.01
Shell floor quarter point region	500	10.11	1.68
Shell floor centerline region	500	8.11	1.11
Cradle above bath level	889	6.08	0.98
Cradle opposite to bath	1915	11.17	1.11
Cradle opposite to metal	2165	16.17	1.61
Cradle opposite to block above bar	818	8.11	1.11
Cradle opposite to block between bars	156	1.17	0.19
Cradle opposite to brick	111	1.80	0.19
Cradle corner	51	1.51	0.15
Cradle below floor close to corner	100	1.76	0.11
Cradle below floor quarter point region	100	1.76	0.11
Cradle below floor centerline region	100	1.76	0.11
Shell end wall opposite to metal	1500	1.61	0.11
Shell end wall opposite to block above bar	1000	7.11	1.18
Shell end wall opposite to block below cap of bar	1000	6.18	1.11
Shell end wall opposite to brick	1000	10.11	1.68
Shell coverplate in the ends	500	1.51	0.15
Shell horizontal stiffeners in the ends	1181	18.00	1.90
Shell vertical stiffeners in the ends	898	5.51	0.89
Shell horizontal stiffeners in the ends	100	0.15	0.01

Total for the cathode part

371.76 59.95

Anode Heat Losses

Cross in side channels	1700	11.18	1.11
Cross above anodes	1800	8.19	1.11
Cross in center channel	1750	1.60	0.58
Scum	1000	17.11	1.18
Yoke	1610	8.17	1.11
Aluminum rod	811	10.11	1.89

Total for the anode part

118.3 10.05

Total for the cell

610.1 100.00

GENSIM

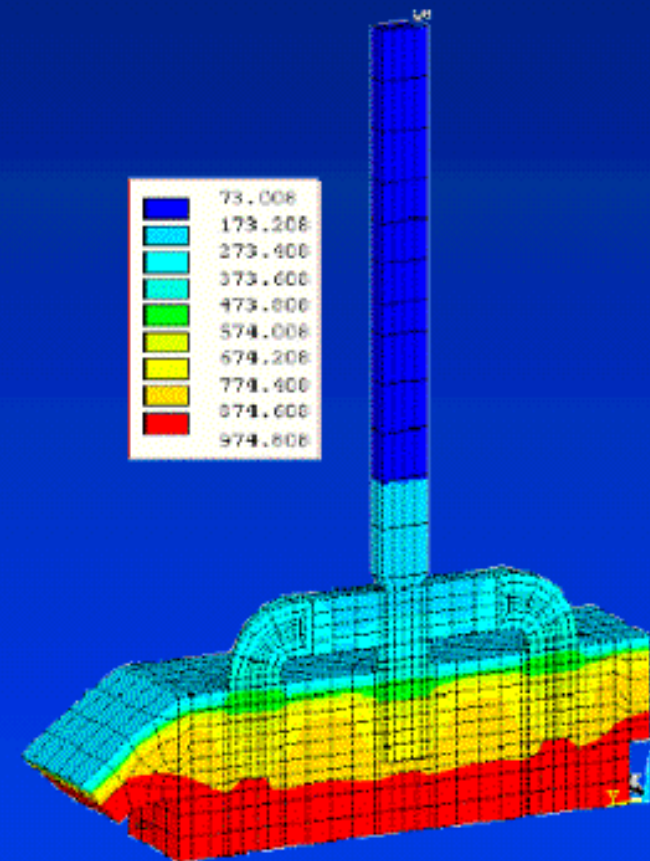
Instrumented Anode Setup



GENTSIM

Half-Anode Model Base Case Results

**** HEAT BALANCE TABLE ****			
**** Half Anode Model : "VAM" 311 ****			
HEAT INPUT	W	W/m ²	2
Bath to anode carbon	1583.54	3538.68	42.86
Bath to crust	613.64	3384.88	38.83
Joule heat	1396.94		39.33
Total Heat Input	3594.12		121.02
HEAT LOST	W	W/m ²	2
Crust to air	1433.63	1691.43	39.35
Studs to air	1839.63	4868.84	49.69
Aluminum rod to air	488.58	693.18	33.36
Total Heat Lost	3761.84		122.40
Solution Error	2.58 E-2		
ANODE PANEL HEAT LOST	W	W/m ²	2
Crust to air	93.15	1691.43	39.35
Studs to air	136.46	4868.84	49.69
Aluminum rod to air	26.34	693.18	33.36
Total Anode Panel Heat Lost	256.05		122.40
Avg. Temp at clamp (mV)	582.383	Current at anode Surf (Amps)	4681.588
Targeted cell current:	500000.00 Amps		
Obtained cell current:	500000.00 Amps		
Solution Error	0.00 E-2		



GENSIM

Cathode Side Slice Model Base Case Results

****	HEAT BALANCE TABLE			****
****	Side Slice Model : "VMA" 388			****
****	Freeze profile converged			****
****	after 7. iterations			****

HEAT INPUT	W	W/m^2	t	

Bath to freeze	745.88	8888.88	17.24	
Metal to freeze	1471.68	14388.86	35.13	
Metal to carbon	1882.48	1687.15	22.57	
Graule heat	1281.75		27.85	

TOTAL HEAT INPUT	4481.81		102.85	

HEAT LOST	W	W/m^2	t	

Shell wall above bath level	641.76	1284.88	14.38	
Shell wall opposite to bath	412.86	5161.22	8.26	
Shell wall opposite to metal	422.58	7828.48	8.48	
Shell wall opposite to block	885.81	5722.22	18.84	
Shell wall below block	84.77	665.54	2.13	
Shell floor	553.18	414.82	7.47	
Cradle above bath level	26.21	1514.87	6.58	
Cradle opposite to bath	181.83	2875.57	2.27	
Cradle opposite to metal	66.45	2546.87	1.48	
Cradle opposite to block	261.83	828.84	5.87	
Cradle opposite to block	43.64	153.86	6.88	
Cradle below floor level	282.55	88.23	4.54	
Gas and flux to air	627.58	2648.48	14.87	
End of flux to busbar	348.32	48514.13	7.63	

TOTAL HEAT LOST	4458.68		102.85	

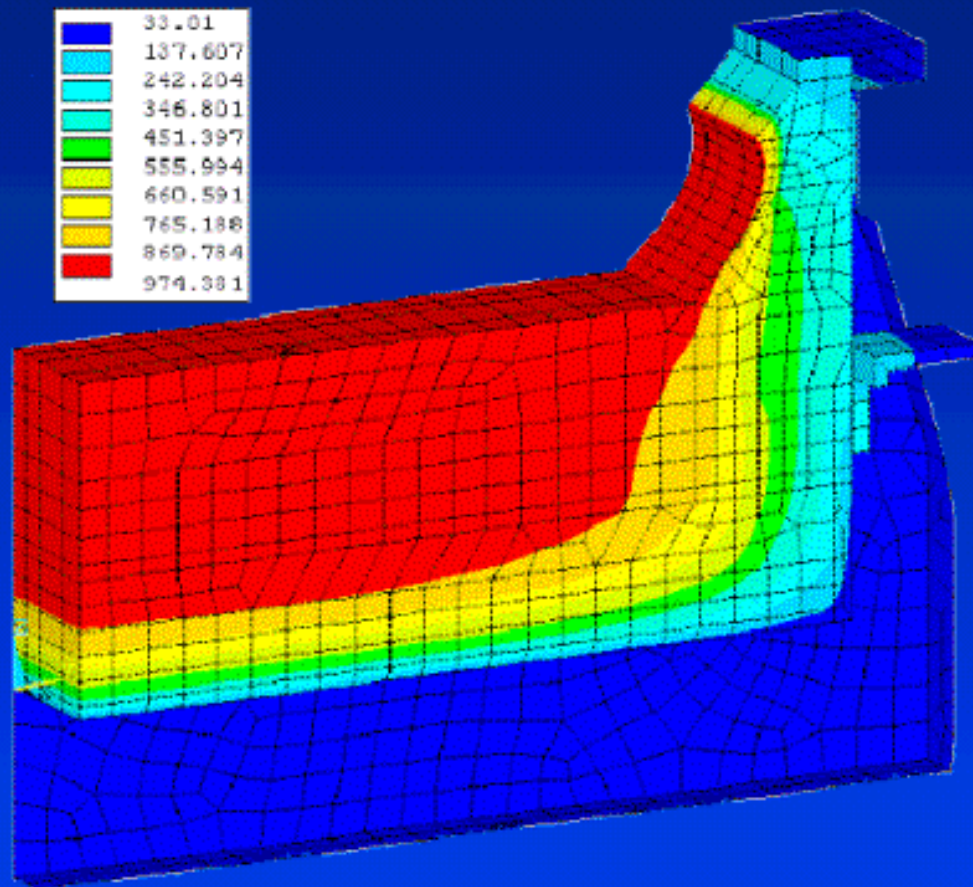
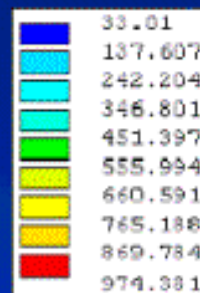
Solution error	1.48 t			

TOTAL CATHODE HEAT LOST	385.52		102.85	

Avg. temp at max end [mV]	Average flux. temp [mV]	Current at Cathode bus [amps]		
-----		-----		
285.268	7.473	4166.667		

targeted cell current:	38888.88	amps		
obtained cell current:	38888.88	amps		

Solution error	1.88 t			



GENTSIM

Comparison Against Cell Internal Heat

```

=====
          ****      HEAT BALANCE SUMMARY      ****
          ****      Full slice Model : "QAM" 200      ****
          ****
=====

INTERNAL HEAT CALCULATION
-----
Bath Resistivity              0.423211 ohm-cm
Anode Current Density         0.732422 A/cm^2
Cathode Current Density       0.668449 A/cm^2
Bath Voltage                  1.57648 volts
Electrolysis Voltage          1.92441 volts
Total Cell Voltage            4.28826 volts
Equivalent Voltage to Make Metal 2.01347 volts
Current Efficiency             92.9152 %
-----
Internal Heat Generation      622.435 kW
=====

TOTAL HEAT LOST
-----
Total Anode Panel Heat Loss   234.350 kW
Total Cathode Heat Loss       285.320 kW
-----
Total Cell Heat Loss          619.670 kW
=====

HEAT UNBALANCE                0.45 %
=====

```

- Bath resistivity using Wang's equation
- Bath voltage using Haupin's equation
- Electrolysis voltage using Haupin's equation
- Equivalent voltage to make metal using Haupin's equation
- Cell current efficiency using Solli's equation

Base Case Data from my CQRDA's Retrofit Study Example

- Base case basic input data:

- amperage 300 kA
- operating temperature 975 °C

- Base case models results:

- cathode lining drop 284 mV
- anode drop 303 mV
- anode panel heat losses 234 kW
- cathode shell heat losses 385 kW

- Base case operational results:

- cell voltage 4.28 V
- internal heat 622.4 kW
- current efficiency 92.91 %
- energy consumption 13.75 kWh / kg

Retrofitted Data from my CQRDA's Retrofit Study Example

- Retrofitted basic input data:

- amperage 265 kA
- operating temperature 950 °C

- Retrofitted models results:

- cathode lining drop 213 mV
- anode drop 276 mV
- anode panel heat losses 183 kW
- cathode shell heat losses 245 kW

- Retrofitted operational results:

- cell voltage 3.85 V
- internal heat 427 kW
- current efficiency 96.0 %
- energy consumption 11.94 kWh / kg

Sensitivity Study Results Summary

- Anode cover reduced from 16 cm to 13 cm
- Model response: anode panel heat losses increased from 235.35 kW to 247.57 kW
- Operating temperature reduced from 975 °C to 973.75 °C
- Model response: cathode shell heat losses reduced from 385.32 kW to 374.62 kW

Verification that the New Thermal Balance have been Found

****	HEAT BALANCE SUMMARY	****
****	Full slice Model : "UAW" 300	****

INTERNAL HEAT CALCULATION		

Bath Resistivity	0.423211	ohm-cm
Anode Current Density	0.732422	A/cm ²
Cathode Current Density	0.668449	A/cm ²
Bath Voltage	1.57648	volts
Electrolysis Voltage	1.92441	volts
Total Cell Voltage	4.28645	volts
Equivalent Voltage to Make Metal	2.01347	volts
Current Efficiency	92.9152	%

Internal Heat Generation	621.293	kW

TOTAL HEAT LOSS		

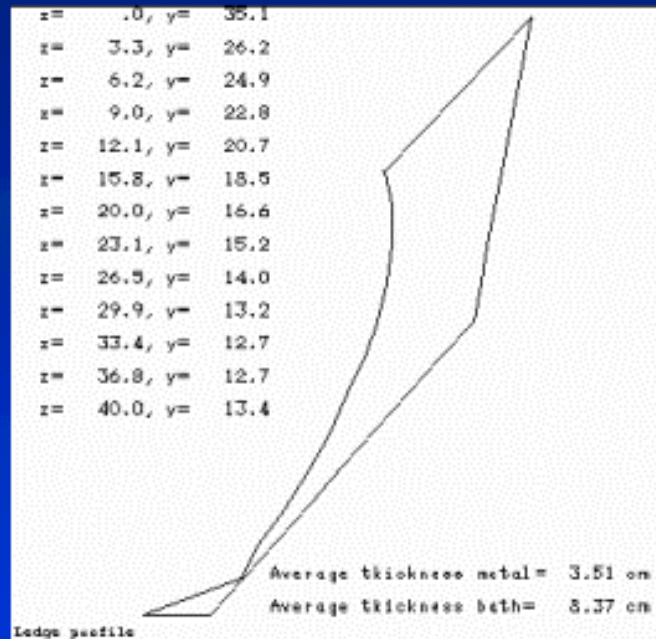
Total Anode Panel Heat Loss	247.570	kW
Total Cathode Heat Loss	374.620	kW

Total Cell Heat Loss	622.190	kW

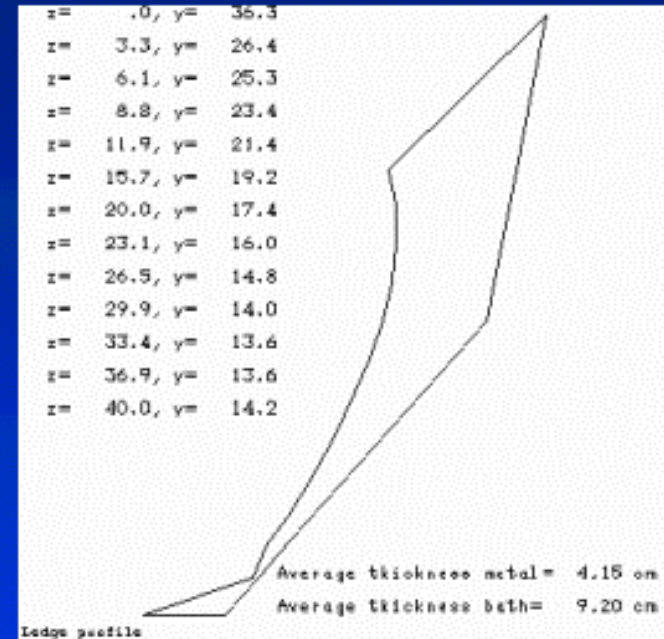
HEAT UNBALANCE	0.05	%
=====		

- With the separated 3D half-anode and 3D cathode side slice models approach, it is up to the user to find the new steady-state operating temperature after having changed the alumina cover thickness
- This can be done by trial and error or by doing some simple "back of the envelope" calculations

Interpretation of the Results



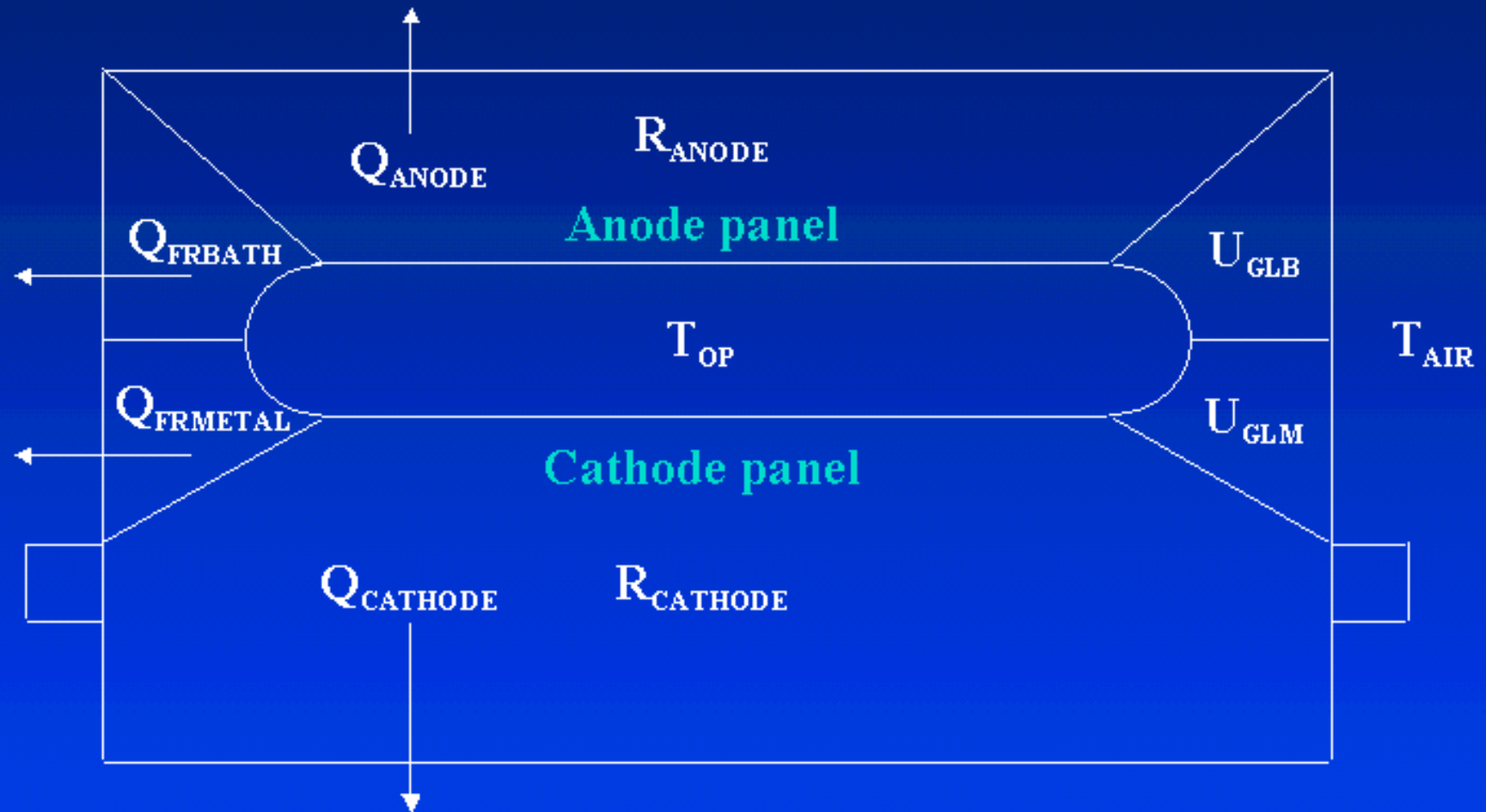
20 °C of cell eutectic superheat



18.75 °C of cell eutectic superheat

- When we remove 3 cm of alumina cover, the cell reacts by increasing the ledge thickness by an average of 0.72 cm

1D Thermal Model Concept



1D Thermal Model Equations

$$Q_{ANODE} = R_{ANODE} * (T_{OP} - T_{AIR})$$

$$Q_{CATHODE} = R_{CATHODE} * (T_{OP} - T_{AIR})$$

$$Q_{FRBATH} = h_{FRB} * A_{BATH \text{ LEDGE}} * (T_{OP} - T_{MLT}) = U_{GLB} * A_{BATH \text{ LEDGE}} * (T_{OP} - T_{AIR})$$

$$Q_{FRMETAL} = h_{FRM} * A_{METAL \text{ LEDGE}} * (T_{OP} - T_{MLT}) = U_{GLM} * A_{METAL \text{ LEDGE}} * (T_{OP} - T_{AIR})$$

$$U_{GLB} = \frac{1}{\left(\frac{1}{U_{FLXB}} + \frac{1}{U_{FRB}} \right)}$$

$$U_{GLM} = \frac{1}{\left(\frac{1}{U_{FLXM}} + \frac{1}{U_{FRM}} \right)}$$

Using the 3D Models Results to Define the Parameters of the 1D Thermal Model

$$Q_{\text{ANODE}} = 234.35 \text{ kW}$$

$$Q_{\text{CATHODE}} = 175.87 \text{ kW}$$

$$R_{\text{ANODE}} = 0.2467 \text{ kW/}^{\circ}\text{C}$$

$$R_{\text{CATHODE}} = 0.1851 \text{ kW/}^{\circ}\text{C}$$

$$Q_{\text{FRBATH}} = 72.31 \text{ kW}$$

$$Q_{\text{FRMETAL}} = 137.14 \text{ kW}$$

$$U_{\text{GLB}} = 10.53 \text{ W/m}^2\text{}^{\circ}\text{C}$$

$$U_{\text{GLM}} = 15.16 \text{ W/m}^2\text{}^{\circ}\text{C}$$

$$U_{\text{FIXB}} = 29.43 \text{ W/m}^2\text{}^{\circ}\text{C}$$

$$U_{\text{FIXM}} = 21.70 \text{ W/m}^2\text{}^{\circ}\text{C}$$

$$U_{\text{FRB}} = 16.39 \text{ W/m}^2\text{}^{\circ}\text{C}$$

$$U_{\text{FRM}} = 50.26 \text{ W/m}^2\text{}^{\circ}\text{C}$$

$$L_{\text{BF}} = 8.26 \text{ cm}$$

$$L_{\text{MF}} = 3.70 \text{ cm}$$

From the 1D Thermal Model Concept to a 1D Thermal Steady-State Model

****	HEAT BALANCE SUMMARY	****
****	Full slice Model : "GEM" 300	****

INTERNAL HEAT CALCULATION		

Bath Resistivity	0.421029 ohm-cm	
Anode Current Density	0.732422 A/cm ²	
Cathode Current Density	0.668449 A/cm ²	
Bath Voltage	1.56835 volts	
Electrolysis Voltage	1.92431 volts	
Total Cell Voltage	4.28004 volts	
Equivalent Voltage to Make Metal	2.01206 volts	
Current Efficiency	92.8436 %	

Internal Heat Generation	620.394 kW	

TOTAL HEAT LOST		

Total Anode Panel Heat Loss	234.114 kW	
Total Cathode Panel Heat Loss	175.693 kW	
Heat Loss Through Ledge at Bath Level	72.702 kW	
Heat Loss Through Ledge at Metal Level	137.886 kW	

Total Cell Heat Loss	620.395 kW	

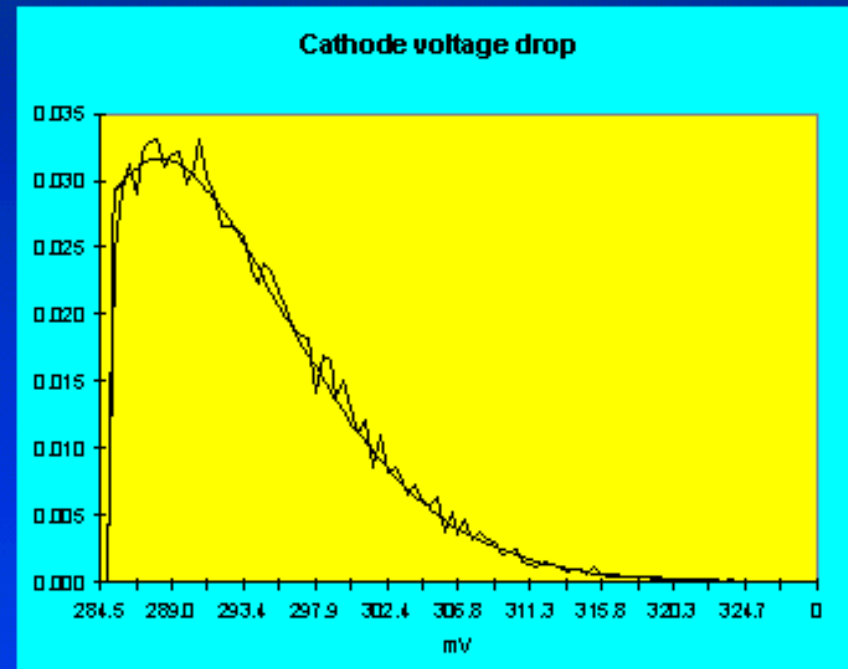
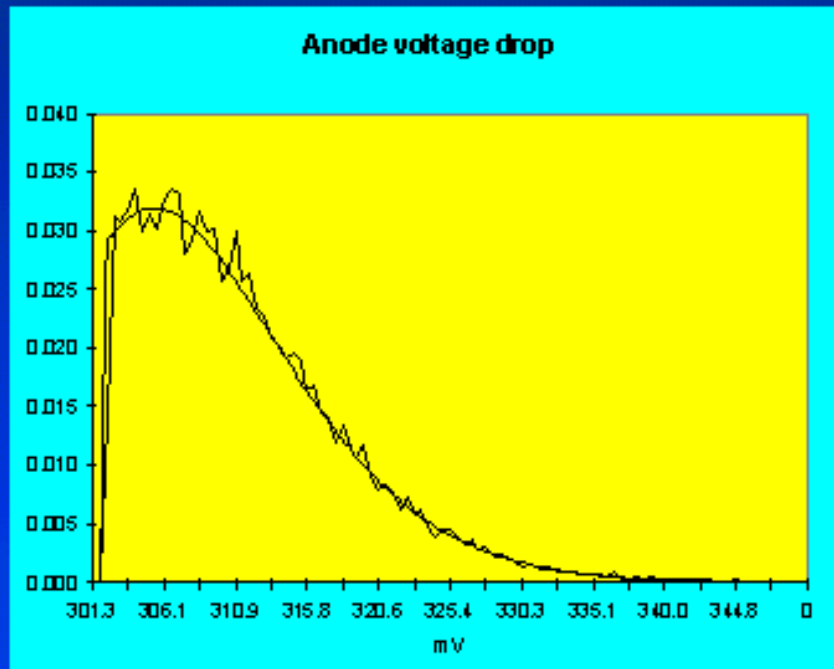
HEAT UNBALANCE	0.00 %	
=====		

Ledge thickness, bath level (cm)	8.60843
Ledge thickness, metal level (cm)	4.04444
Bath chemistry:	
Cryolite ratio	2.50691
Bath ratio	1.25345
Modified conc. of diss. alumina (%)	1.23832
Conc. of diss. alumina at eubect. (%)	7.48812
Conc. of saturated diss. alumina (%)	8.53723
Conc. of cryolite (%)	87.70000
Heat balance:	
Superheat (C)	19.4736
Cell energy consumption (kWh/kg)	13.7405
Total side resist. bath level (W/m ² C)	10.260
Total side resist. met. level (W/m ² C)	14.774
Total heat loss (kW)	620.395
Total electrical input energy (kW)	1224.01
Internal heat generation (kW)	620.394
Electrical characteristics:	
Current efficiency (%)	92.8436
Cathode current density (A/cm ²)	0.732422
Cathode current density (A/cm ²)	0.668449
Bath resistivity (ohm-cm)	0.421029
Cell pseudo-resistance (micro-ohm)	8.76679
Bath voltage (V)	1.56835
Electrolysis voltage (V)	1.92431
Cell voltage (V)	4.28004
Voltage to make the metal (V)	2.01206
Geometric variables:	
Area of anodes (m ²)	40.9600
Perimeter of ledge, bath level (m)	35.5557
Perimeter of ledge, metal level (m)	35.1222

Prediction of the 1D Steady-State Model for the Sensitivity Study

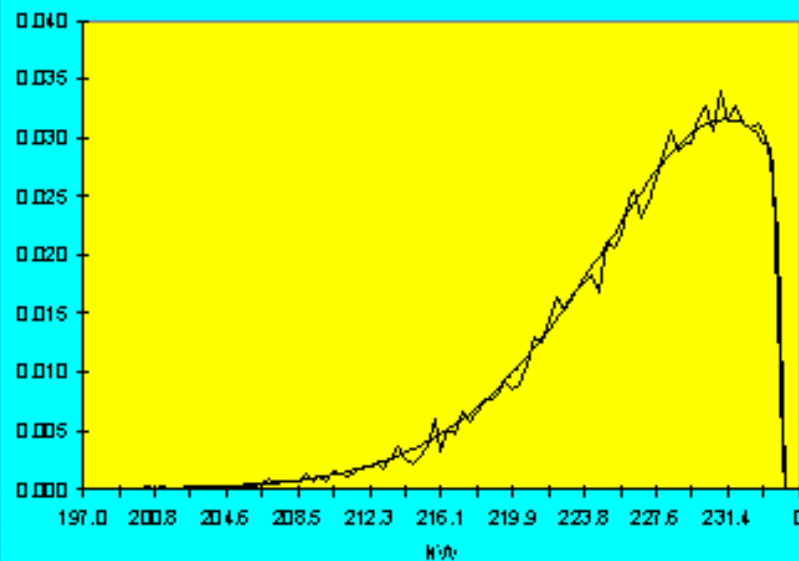
- | | | |
|--------------------------------------|---|-----------|
| ● Thickness of anode cover: | 16 cm | 13 cm |
| ● Anode panel heat loss at 975 °C : | 234.35 kW | 247.57 kW |
| ● Converged operating temperature: | 974.05 °C | 972.89 °C |
| ● Converged cell eutectic superheat: | 19.47 °C | 18.32 °C |
| ● Converged bath's ledge thickness: | 8.61 cm | 9.45 cm |
| ● Converged metal's ledge thickness: | 4.04 cm | 4.88 cm |
| ● Conclusion of the study: | an average of 0.84 cm extra ledge thickness | |

Monte Carlo Sensitivity Study: Replace Definite Results Obtained by 3D Models by Probability Distributions

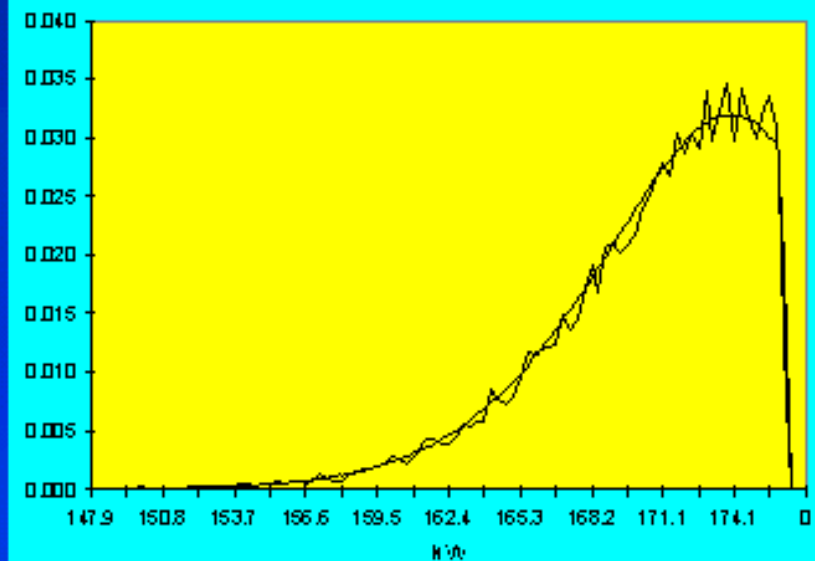


Monte Carlo Sensitivity Study: Replace Definite Results Obtained by 3D Models by Probability Distributions

Anode panel heat loss

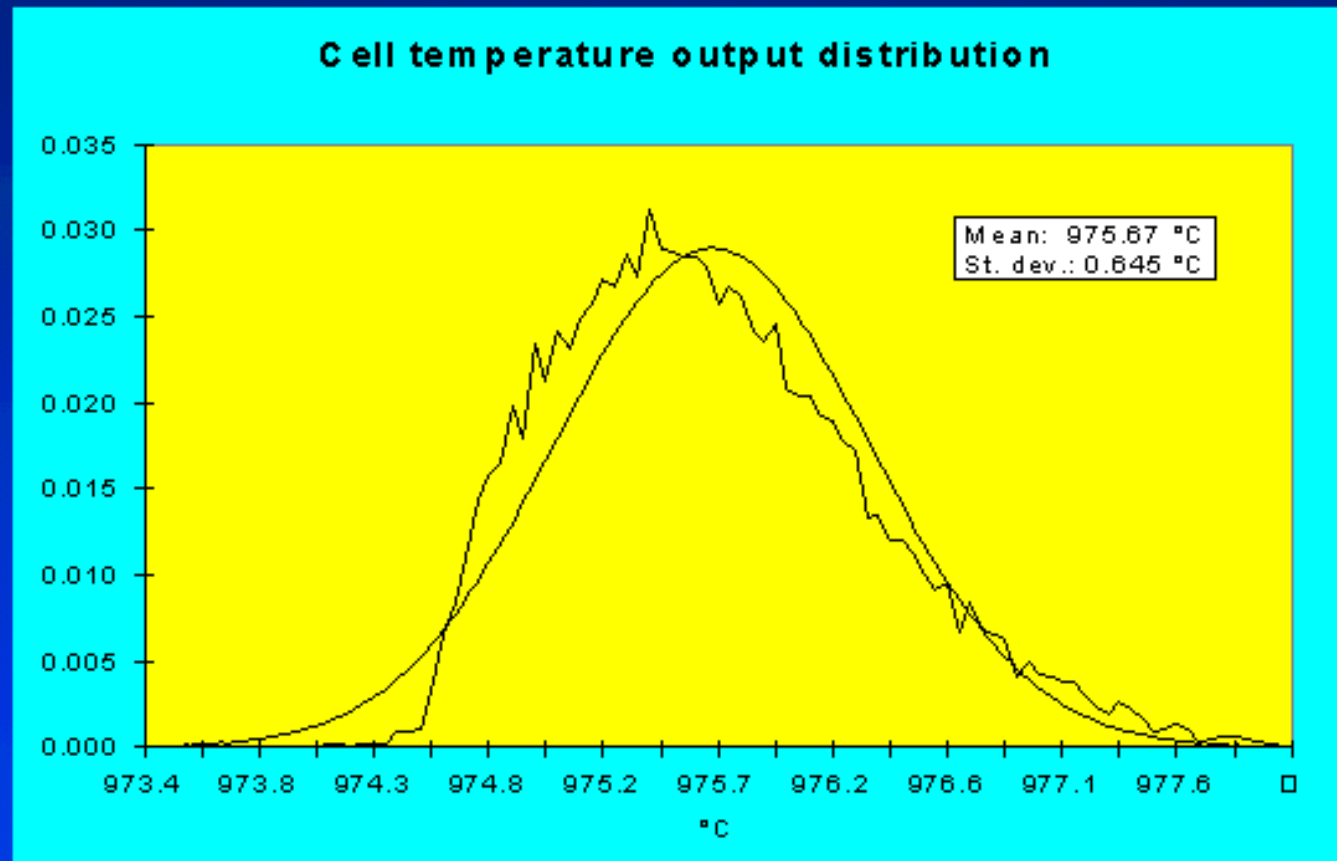


Cathode panel heat loss



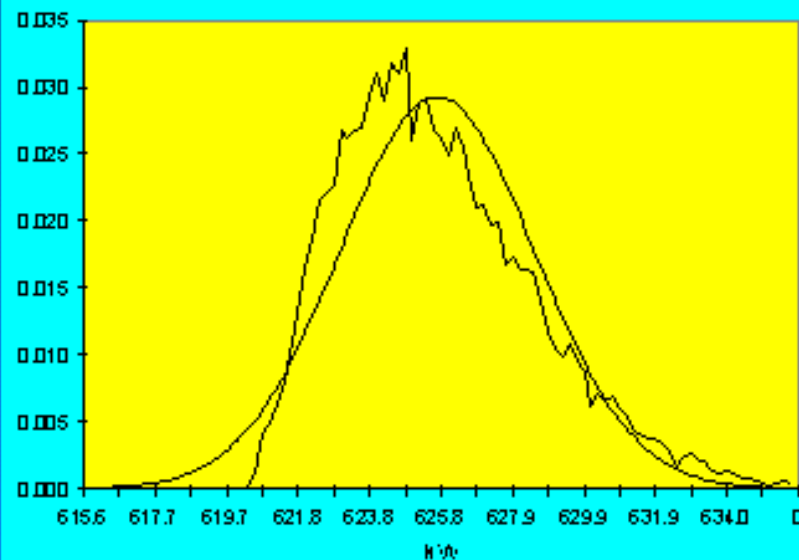
GENISIM

Main Output Distribution of the Monte Carlo Study

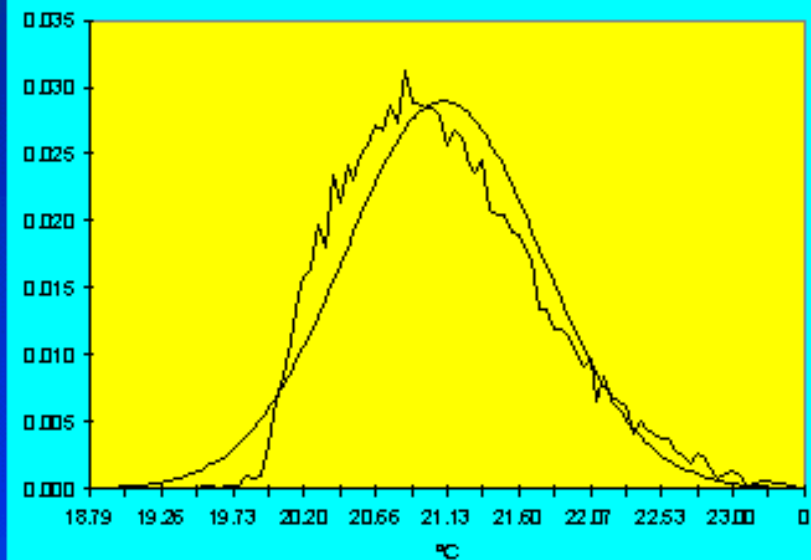


Indirect Output Variable Distributions from the Monte Carlo Study

Internal heat output distribution

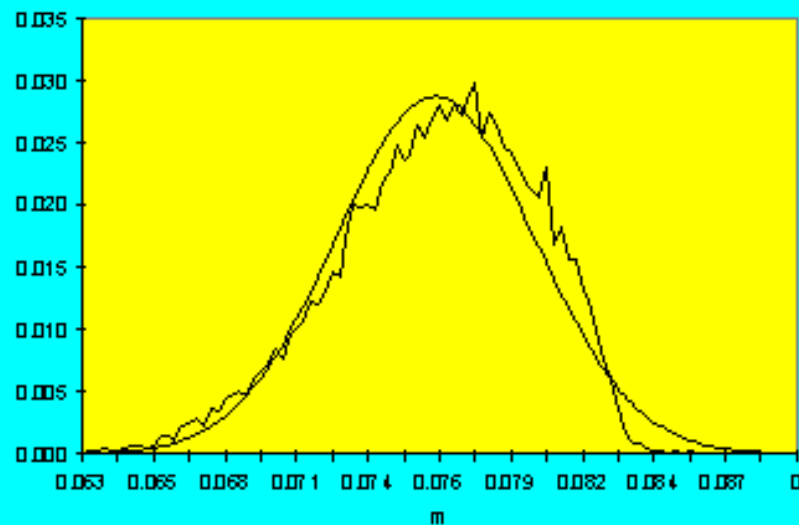


Eutectic superheat output distribution

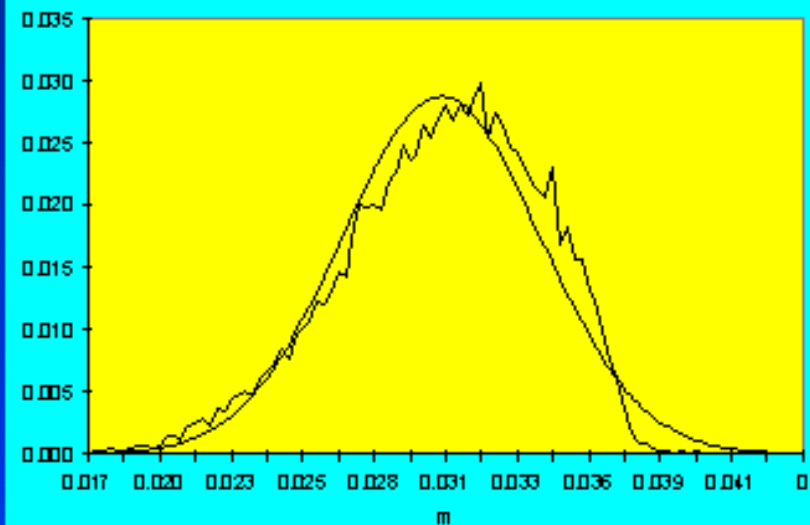


Indirect Output Variable Distributions from the Monte Carlo Study

Ledge thickness at bath level
output distribution



Ledge thickness at metal level
output distribution



Extending from a 1D Steady-State Model to a 1D Dynamic Model

Adding to the Process Model

- Mass balance equations of all the constituents of the bath, the dispersed alumina, the sludge and the metal
- Kinetic equations of the alumina dissolution, sludge formation, back feeding and metal production reaction
- Kinetic equation of the ledge formation and melting, and equations that follow the dynamic ledge thickness evolution both at bath and metal level
- Kinetic equation of the fluoride evaporation
- Equation that follows the ACD dynamic evolution

Extending from a 1D Steady-State Model to a 1D Dynamic Model

Additions to the Heat Balance Equation

- **Splitting of the energy required to make metal terms into 3 components:**
 - the energy required to heat-up to bath temperature and dissolve the alumina
 - the energy required to heat-up to bath temperature the anode carbon block
 - the energy required by the chemical reaction itself
- **Adding terms to account for the heat required to heat-up and to dissolve all additives fed to the cell. For the alumina, the heat required to dissolve it is coupled to its rate of dissolution.**

Extending from a 1D Steady-State Model to a 1D Dynamic Model

Additions to the Heat Balance Equation

- Adding a term to account for the heat required to heat-up newly set anodes including a kinetic equation for its heating rate
- Adding a term to account for the heat of fusion of the ledge that is coupled to its forming/melting rate
- Adding a term for the latent heat of the bath, metal, dispersed alumina and sludge

Extending from a 1D Steady-State Model to a 1D Dynamic Model

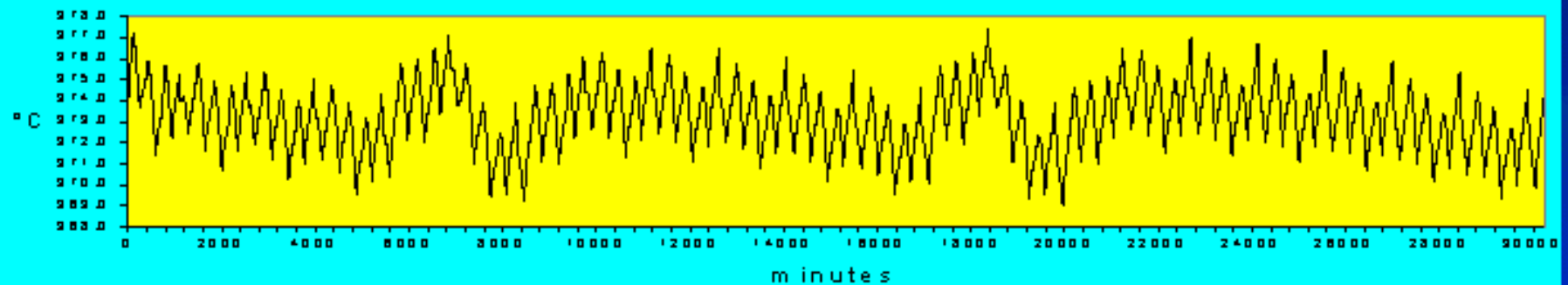
Adding a Control Model

- Cell alumina feeding and cell resistance control algorithm
- Anode effect quenching control algorithm
- Bath ratio control logic
- Metal tapping policy
- Anode change schedule

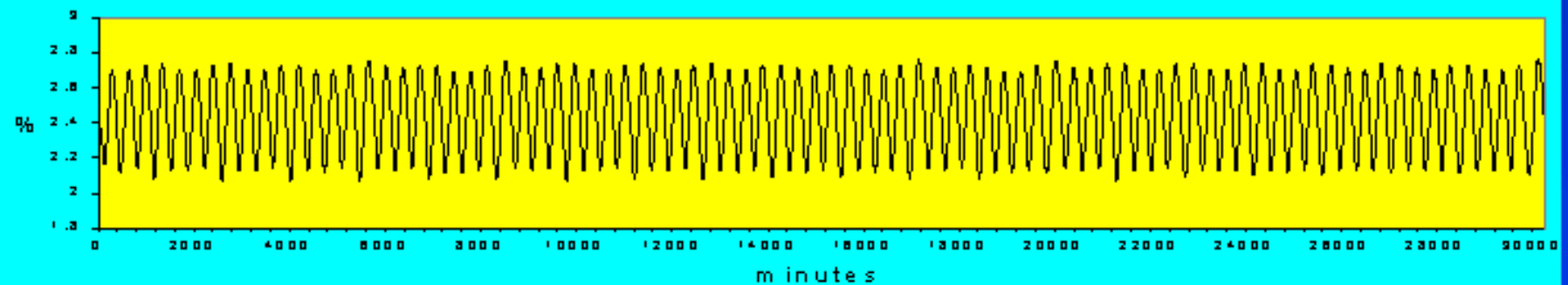
1D Dynamic Model Application

3 Weeks of Stable Operation

Cell temperature evolution



Dissolved alumina evolution

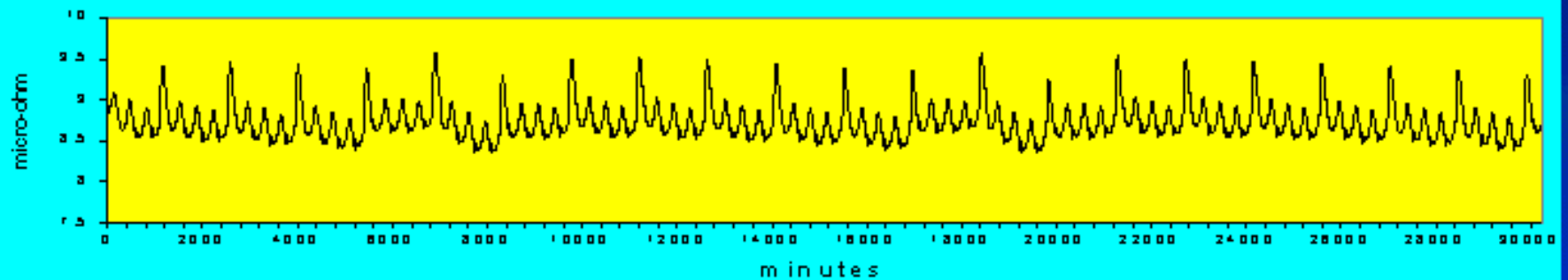


GENISIM

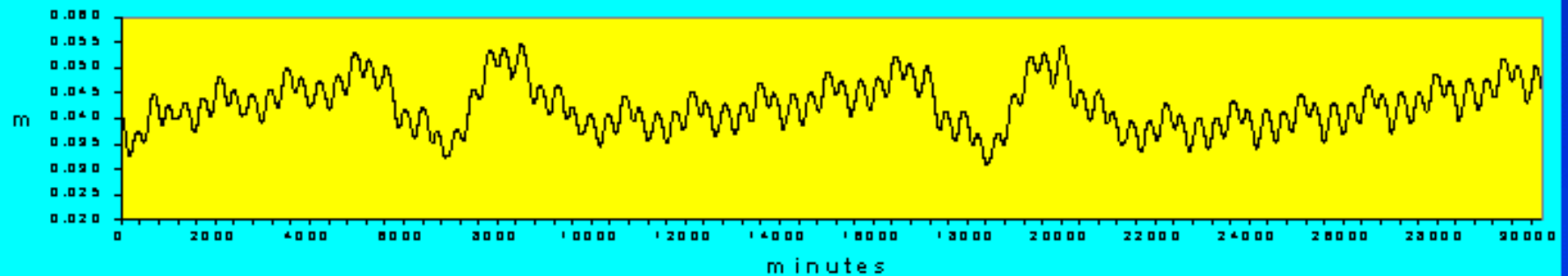
1D Dynamic Model Application

3 Weeks of Stable Operation

Pseudo-resistance evolution



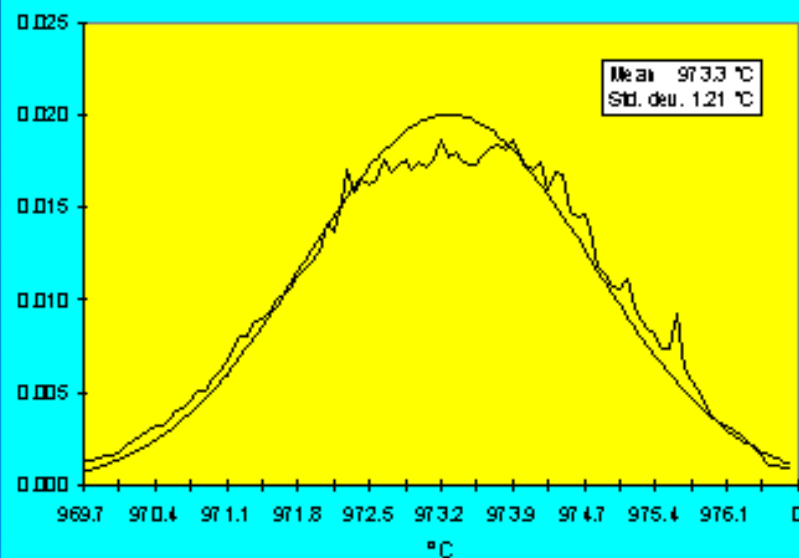
Ledge thickness at metal level evolution



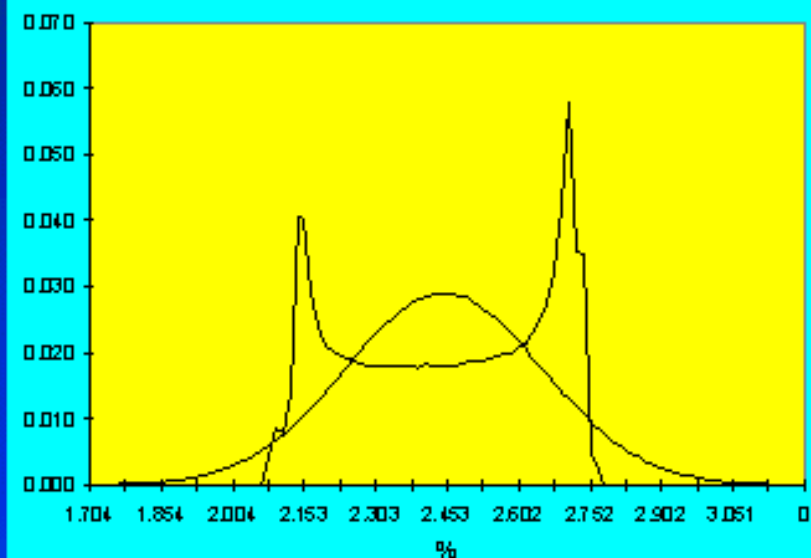
GENISIM

Histograms from the Dynamic Model for Stable Cell Operation

Temperature dynamic distribution

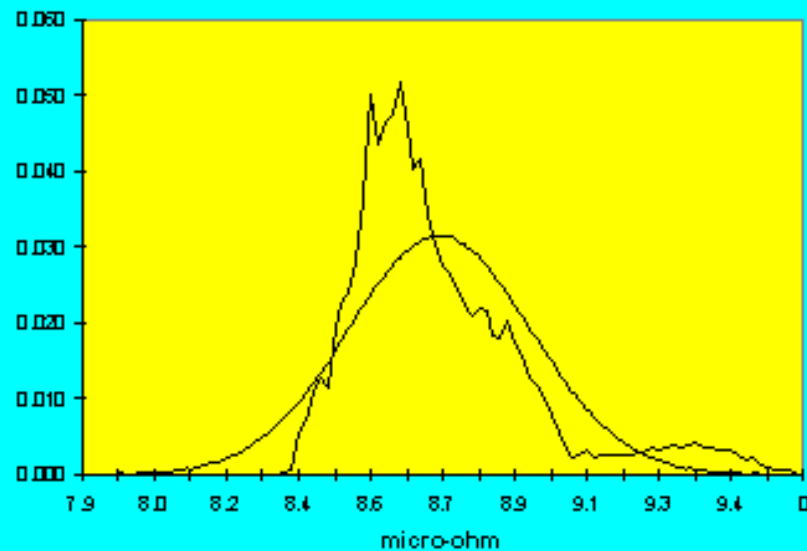


Dissolved alumina dynamic distribution

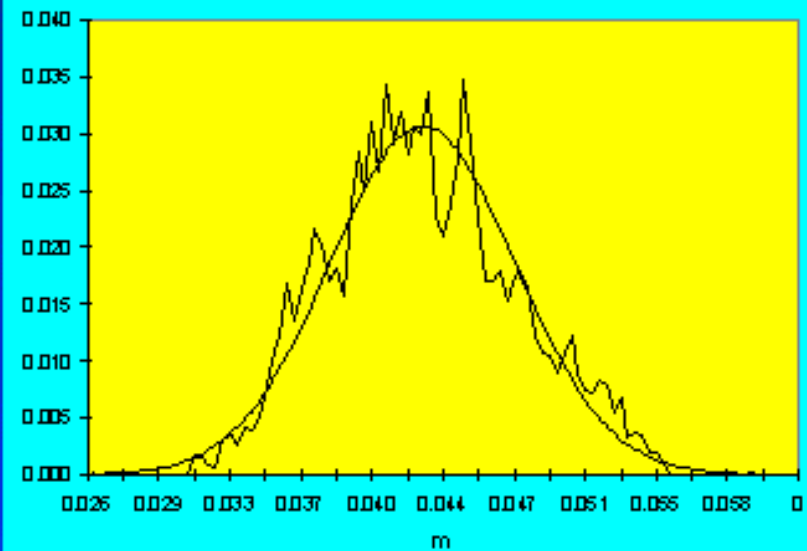


Histograms from the Dynamic Model for Stable Cell Operation

Cell pseudo-resistance dynamic distribution



Ledge metal level dynamic distribution



Conclusions from the Monte Carlo and Dynamic Study

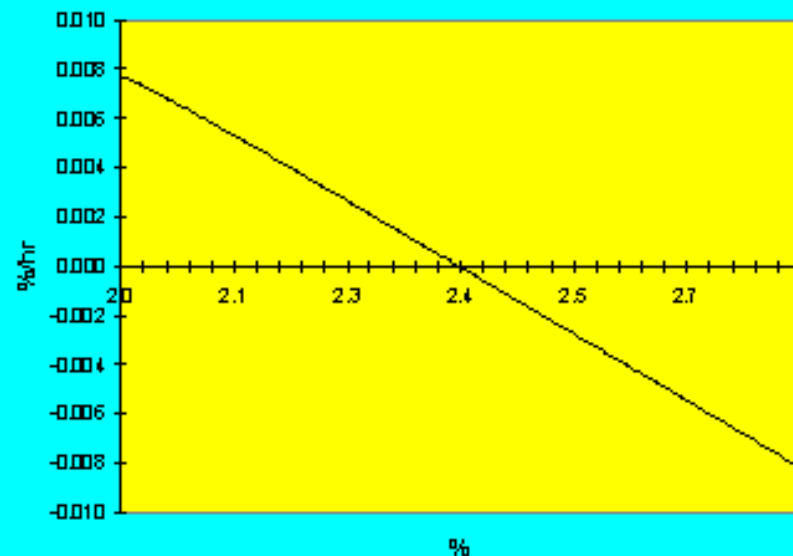
By designing a cell to have 4 cm of ledge in the 3D steady-state model, we have a fair amount of chance to end up with a cell having only 2 cm of ledge left in its normal "low tide" conditions!

Knowing that, it is up to the design team to decide if 4 cm of ledge at the metal level is a safe target for the 3D steady-state model "Optimal Design Solution"

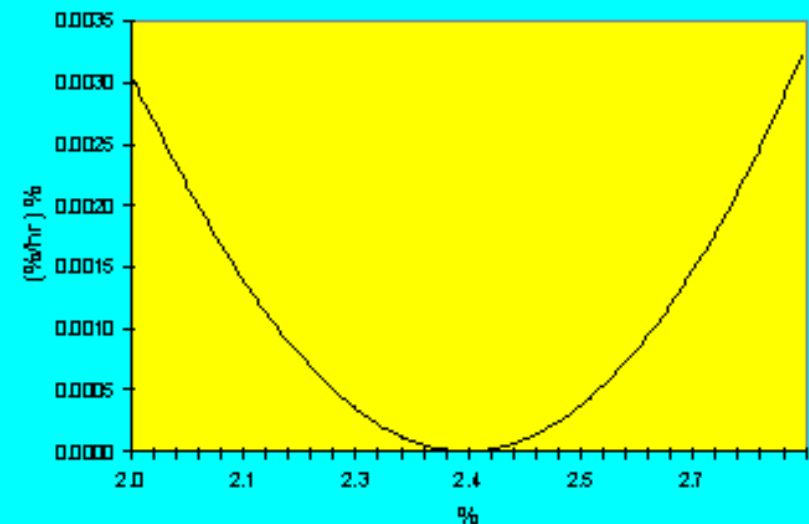
Using a 1D Dynamic Model to Assist in the Development of Cell Control Logic

Theory A: Positive CE vs. $\%Al_2O_3$ Slope

Rate of change of $\%CAI203$ vs $\%CAI203$



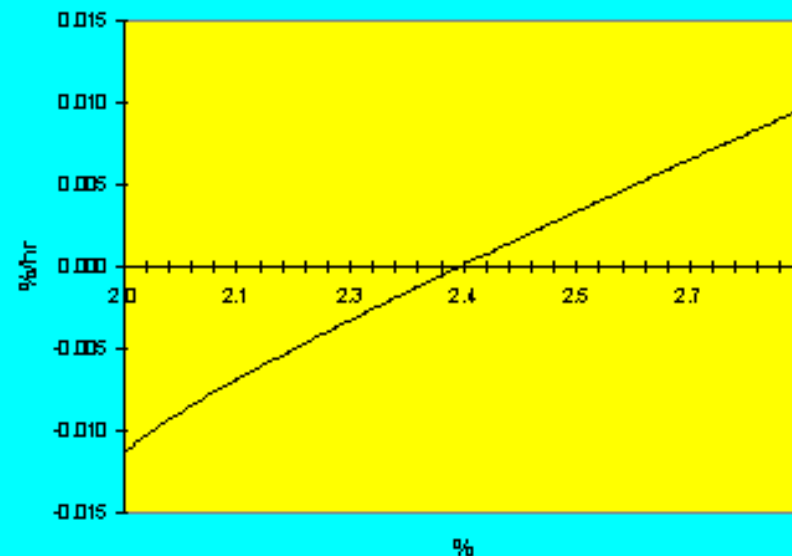
Rate of change of $\%CAI203 * \%CAI203$ offset vs $\%CAI203$



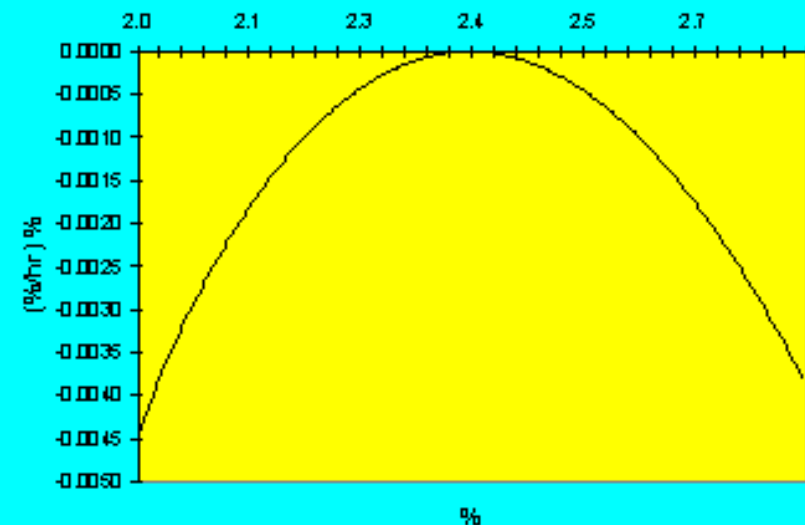
Using a 1D Dynamic Model to Assist in the Development of Cell Control Logic

Theory B: Negative CE vs. $\%Al_2O_3$ Slope

Rate of change of $\%CAI203$ vs $\%CAI203$



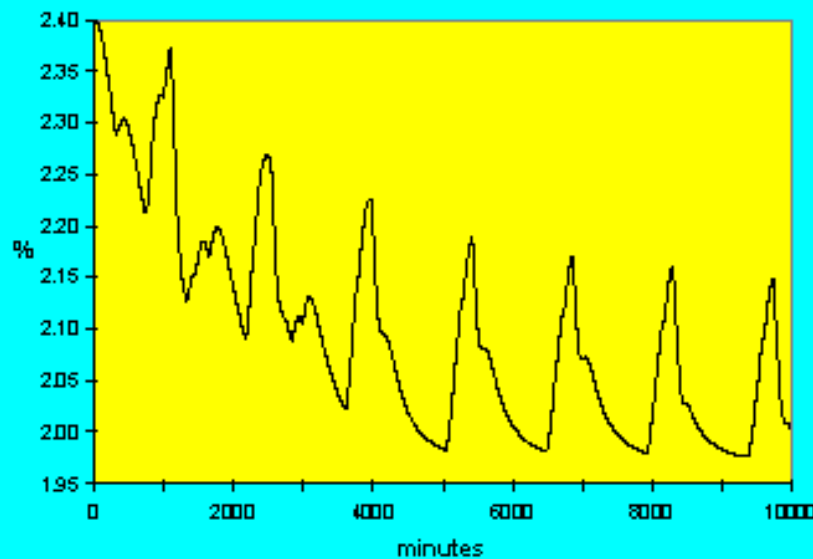
Rate of change of $\%CAI203 * \%CAI203$ offset vs $\%CAI203$



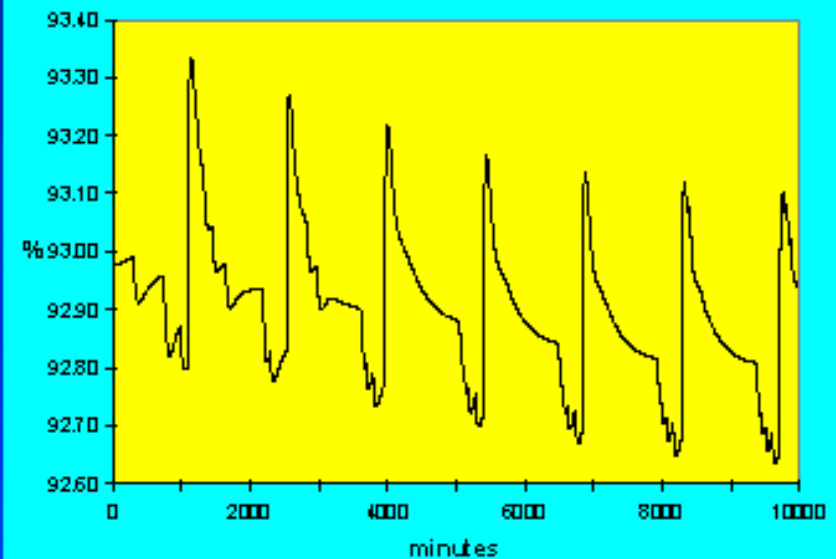
Using a 1D Dynamic Model to Assist in the Development of Cell Control Logic

Theory A: Nominal Feeding at 179.5 kg/hr

Dynamic %CAI2O3 evolution



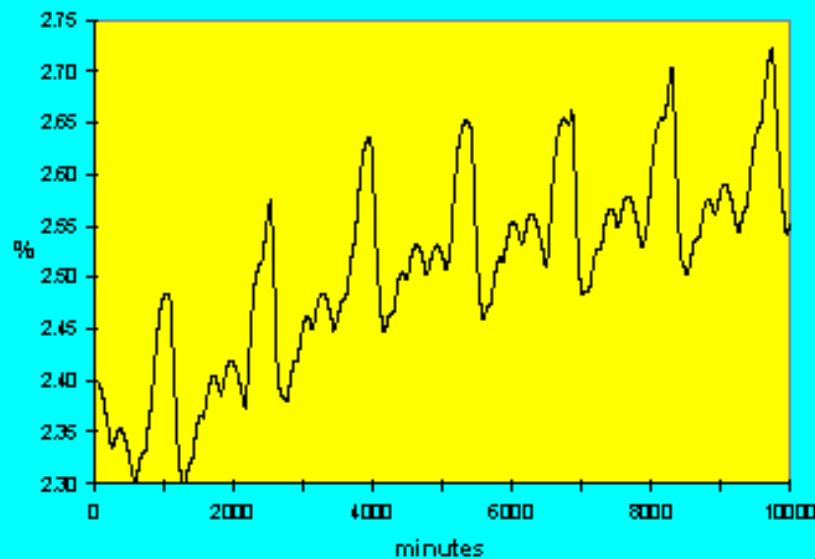
Dynamic %CE evolution



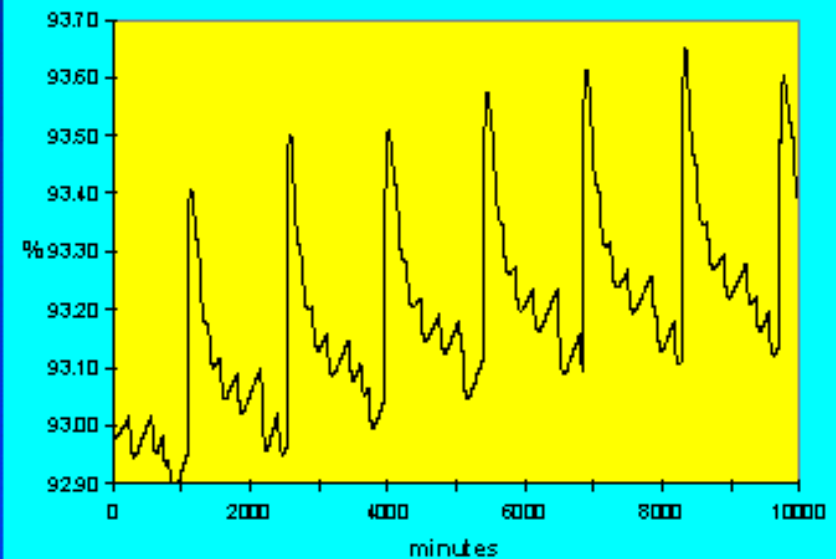
Using a 1D Dynamic Model to Assist in the Development of Cell Control Logic

Theory A: Nominal Feeding at 180.5 kg/hr

Dynamic %CAI203 evolution



Dynamic %CE evolution



Using a 1D Dynamic Model to Assist in the Development of Cell Control Logic

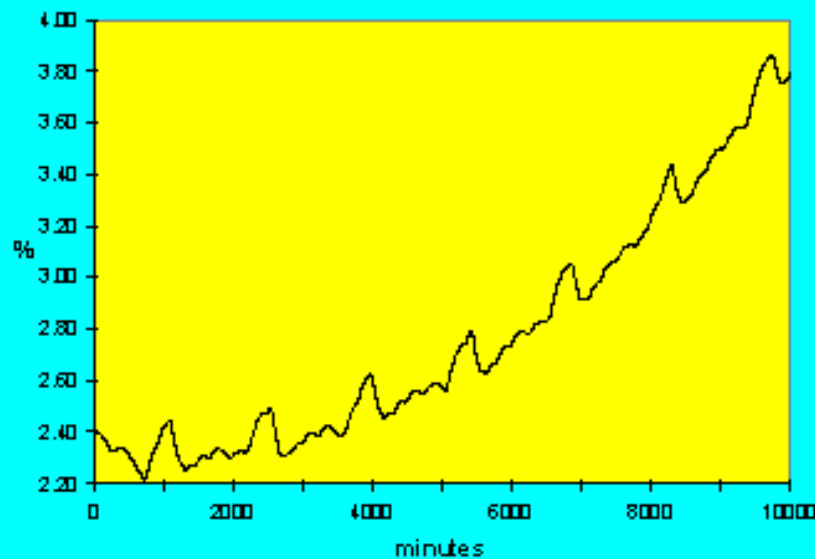
Nominal feeding logic is perfectly adapted to the case where the slope of the CE vs. Al_2O_3 is positive because:

- It is advantageous to operate constantly the cell at a nominal rate that corresponds to an alumina concentration of around 3.5 % maximizing both the current efficiency and the power efficiency
- The cell is "self-compensating" small fluctuations in the targeted feeding rate

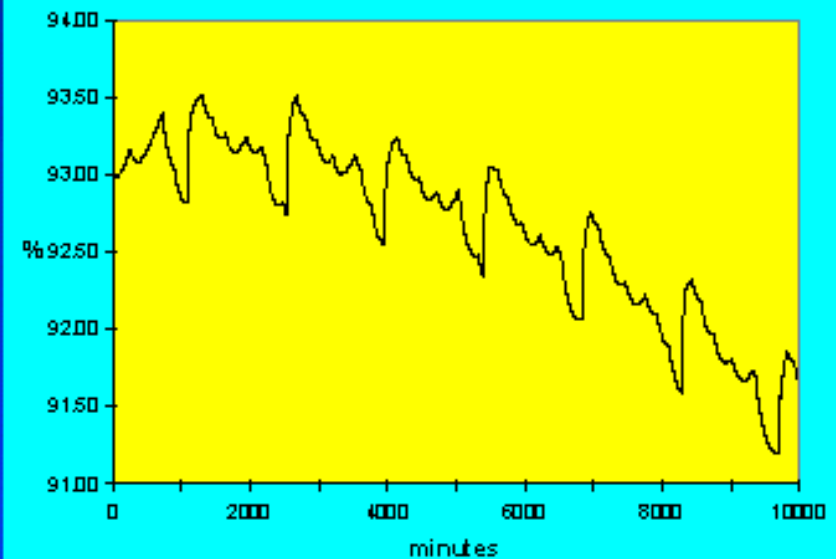
Using a 1D Dynamic Model to Assist in the Development of Cell Control Logic

Theory B: Nominal Feeding at 180.5 kg/hr

Dynamic %CAI203 evolution



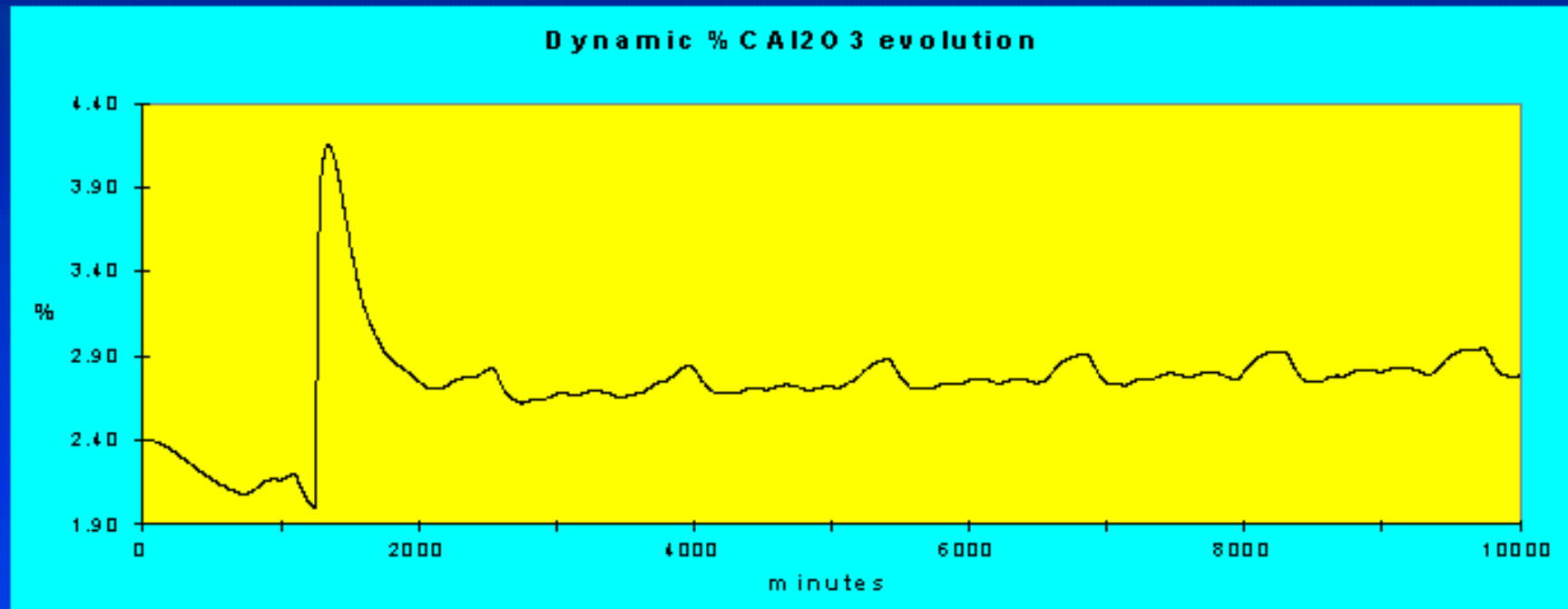
Dynamic %CE evolution



GENISIM

Using a 1D Dynamic Model to Assist in the Development of Cell Control Logic

Theory B: Nominal Feeding at 179.5 kg/hr

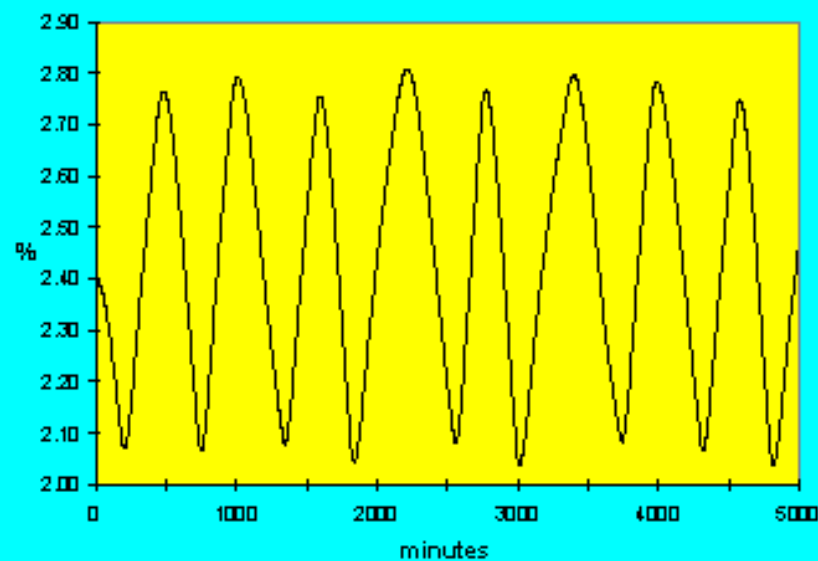


GENISIM

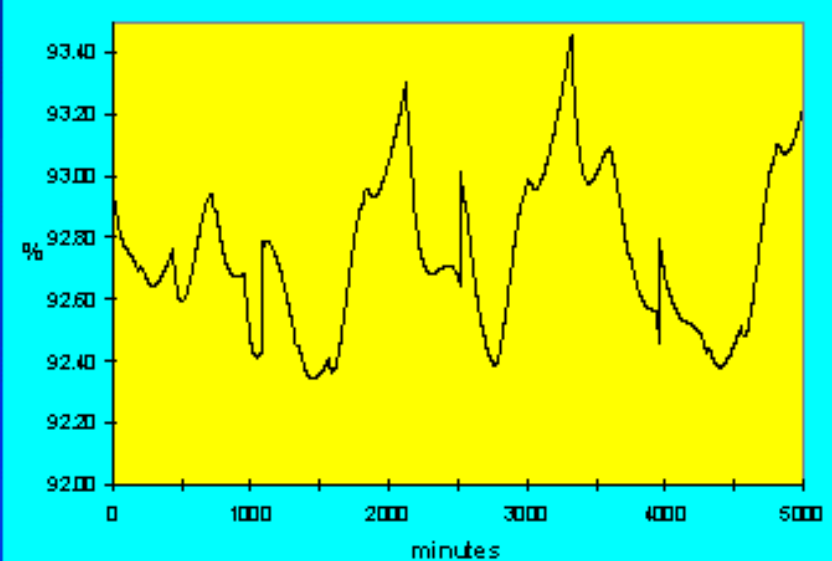
Using a 1D Dynamic Model to Assist in the Development of Cell Control Logic

Theory B: Continuous Tracking

Dynamic %CAI203 evolution



Dynamic %CE evolution



Using a 1D Dynamic Model to Assist in the Development of Cell Control Logic

Continuous tracking feeding logic is perfectly adapted to the case where the slope of the CE vs. Al_2O_3 is negative because:

- Knowing that a steady-state nominal feeding rate does not exist, it instead maintains a continuous balancing act by shifting between strong over and under-feeding rate
- It maintains the alumina concentration at its minimum in order to maximize the cell current efficiency and at the same time takes advantage of the cell resistance increased toward the anode effect to evaluate when it is time to change the alumina feeding rate.

Conclusions

In general conclusion, I hope I was able to convince you of the value of using process simulation models to assist you in your work, since I strongly believe that they offer tremendous opportunities to improve the productivity of all of the smelters in operation today